Faculty of Engineering Smgrc Group	Intelligent Control	
Fall 2023	Assignment Fuzzy rules and fuzzy inference engine Fuzzification and defuzzification	VES V
Dr. Poymoni		University of Kurdistan

	Γ	Dr.]	. в Ba	igz	ra zao	nı le	: h				D	ea	ad	li	ne):	24	4]	N	OV	•									
																														_
						T																								

1- Suppose that a fuzzy rule base consists of two rule:

$$\begin{cases} \text{IF } x_1 \text{ is } A_1 \text{ and } \cdots \text{ and } x_n \text{ is } A_n \text{ THEN } y \text{ is } B \\ \text{IF } x_1 \text{ is } C_1 \text{ and } \cdots \text{ and } x_n \text{ is } C_n \text{ THEN } y \text{ is } D \end{cases}$$

where

$$\mu_B(y) = \begin{cases} 1 - |y| & |y| \le 1 \\ 0 & o.w. \end{cases} \text{ and } \mu_D(y) = \begin{cases} 1 - |y-1| & |y-1| \le 1 \\ 0 & o.w. \end{cases}$$

and let $\mu_A(x^*) = \prod_{i=1}^n \mu_{A_i}(x_i^*)$ and $\mu_C(x^*) = \prod_{i=1}^n \mu_{C_i}(x_i^*).$

- a) Obtain $\mu_{B'}(y)$ by using the singleton fuzzifier and product inference engine.
- b) Calculate the fuzzy system output y^* by employing center average defuzzifier and maximum defuzzifier.
- 2- Suppose that a fuzzy rule base consists of the M rules:

IF
$$x_1$$
 is A_1^l and \cdots and x_n is A_n^l THEN y is B^l

where

$$\mu_{A_i^l}(x_i) = \begin{cases} 1 - \frac{x_i - \overline{x}_i^l}{\sigma_i^l} & \left| x_i - \overline{x}_i^l \right| \le \sigma_i^l \\ 0 & o.w. \end{cases}$$

and that we use the triangular fuzzifier. Determine the output of the fuzzy inference engine $\mu_{B'}(y)$ for:

- a) product inference engine with algebraic product t-norm.
- b) minimum inference engine with minimum t-norm.