



1- Suppose that a fuzzy rule base consists of two rule:

$$\begin{cases} \text{IF } x_1 \text{ is } A_1 \text{ and } \dots \text{ and } x_n \text{ is } A_n \text{ THEN } y \text{ is } B \\ \text{IF } x_1 \text{ is } C_1 \text{ and } \dots \text{ and } x_n \text{ is } C_n \text{ THEN } y \text{ is } D \end{cases}$$

where

$$\mu_B(y) = \begin{cases} 1 - |y| & |y| \leq 1 \\ 0 & o.w. \end{cases} \quad \text{and} \quad \mu_D(y) = \begin{cases} 1 - |y - 1| & |y - 1| \leq 1 \\ 0 & o.w. \end{cases}$$

and let $\mu_A(x^*) = \prod_{i=1}^n \mu_{A_i}(x_i^*)$ and $\mu_C(x^*) = \prod_{i=1}^n \mu_{C_i}(x_i^*)$.

- Obtain $\mu_{B'}(y)$ by using the singleton fuzzifier and product inference engine.
- Calculate the fuzzy system output y^* by employing center average defuzzifier and maximum defuzzifier.

2- Suppose that a fuzzy rule base consists of the M rules:

$$\text{IF } x_1 \text{ is } A_1^l \text{ and } \dots \text{ and } x_n \text{ is } A_n^l \text{ THEN } y \text{ is } B^l$$

where

$$\mu_{A_i^l}(x_i) = \begin{cases} 1 - \frac{|x_i - \bar{x}_i^l|}{\sigma_i^l} & |x_i - \bar{x}_i^l| \leq \sigma_i^l \\ 0 & o.w. \end{cases}$$

and that we use the triangular fuzzifier. Determine the output of the fuzzy inference engine $\mu_{B'}(y)$ for:

- product inference engine with algebraic product t-norm.
- minimum inference engine with minimum t-norm.